

A cat is a cat and a Euro is a Euro, not (?)¹

An assessment of AI/ML methods applied to Asset Allocation

Bernhard Pfaff

Invesco Asset Management GmbH, 60322 Frankfurt am Main
bernhard.pfaff@invesco.com

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¹Quote: 'a Euro is a Euro' by Willem F. Duisenberg, [ECB Press Conference](#), 4th February 1999.

Introduction

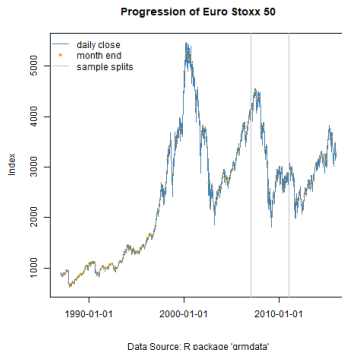
- First wave of ML-/AI methods applied to problems in finance dates back to the 1990s and was inspired by applications in the field of engineering (quality control), e.g., Karlsruher Ökonometrie Workshops, see Bol, Nakhaeizadeh, and Vollmer [1994](#); Bol, Nakhaeizadeh, and Vollmer [1996](#); Bol, Nakhaeizadeh, and Vollmer [2000](#).
- Second wave (attempt) of applying ML-/AI-method to problems in finance since the mid 2010s and was motivated by successful applications in image/video classification, NLP, *etc.*
- What has changed in the interim?
 - ① Computational capacity.
 - ② Count of data records/observations.
 - ③ Access to 'ready-made' software implementations, e.g. Chollet and Allaire [2018](#).
- Will this second wave last and form a new paradigm?²

²Kuhn [1970](#).

The Challenge

Euro Stoxx 50 Index

- Binary classification:
Predict sign of subsequent monthly returns (aka as *label*).
- Use trailing daily observations for defining explanatory variables (aka as *features*).
- Sample Split:
 - 1 Training:
31.01.1987 – 31.12.2006.
 - 2 Validating:
31.01.2007 – 31.12.2010.
 - 3 Testing:
31.01.2011 – 31.12.2015.



The Challenge

The Peer Models/Methods

- 1 Linear Discriminant Analysis: Fisher [1936](#)
- 2 k-Nearest Neighbours: Hart [1968](#)
- 3 Support Vector Machines: Vapnik and Lerner [1963](#); Vapnik and Chervonenkis [1974](#); Vapnik [1995](#); Vapnik, Golowich, and Smola [1997](#)
- 4 Classification Trees: Breiman et al. [1984](#)
- 5 Random Forest: Kleinberg [1990](#); Kleinberg [1996](#); Kleinberg [2000](#); Ho [n.d.](#); Ho [1998](#); Breiman [2001](#)
- 6 (Extreme) Gradient Boosting: Friedman [2001](#); Friedman [2002](#)
- 7 Feed-Forward Neural Networks: Chollet and Allaire [2018](#); Goodfellow [2016](#); Prado [2018](#); Rosenblatt [1958](#); Russell [2010](#)

The Features

Alternative Momentum Measures

- 1 Sign of (significant) slope coefficient in local trend regression;
set of indicator values $\{-1, 0, 1\}$.
- 2 Two-part trend (last five and ten trading days in a month) based on simple moving averages;
set of indicator values $\{-1, 0, 1\}$.
- 3 Relative strength index (RSI) with hurdles 30 and 70;
set of indicator values $\{-1, 0, 1\}$.
- 4 Trend Detection Index (TDI) derived from last ten trading days in a month;
set of indicator values $\{-1, 0, 1\}$.

The Features

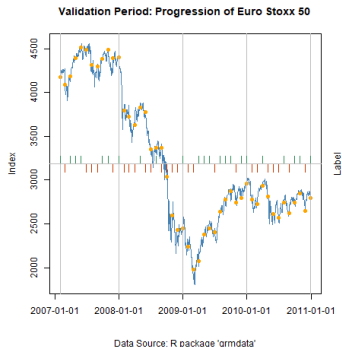
Alternative Risk Measures

- 1 Standard deviations of intra-month daily returns (last ten trading days vs. all observations);
set of indicator values $\{-1, 1\}$.
- 2 Realized volatility of intra-month daily returns (last ten trading days vs. all observations);
set of indicator values $\{-1, 1\}$.
- 3 Sharpe ratio (last ten trading days vs. all observations);
set of indicator values $\{-1, 1\}$.
- 4 Sign of skewness of intra-month daily returns;
set of indicator values $\{-1, 1\}$.
- 5 Sign of excess kurtosis of intra-month daily returns;
set of indicator values $\{-1, 1\}$.

Model Training

Outline

- Each specified model is trained on the training set, and evaluated by its predictive accuracy on the validation set.
- An extending recursive training/shrinking validation set by 12 months is utilized.
- The model specification of a ML-method with the highest hit rate is used for the test set.



Model Training

Linear Discriminant Analysis

LDA models	Validation Periods				Average
	48 Months	36 Months	24 Months	12 Months	
Method = moment, DF = NA	54.2	55.6	45.8	41.7	49.3
Method = mle, DF = NA	54.2	55.6	45.8	41.7	49.3
Method = t, DF = 5	56.2	52.8	45.8	50.0	51.2
Method = t, DF = 10	56.2	52.8	45.8	50.0	51.2
Method = t, DF = 15	56.2	52.8	45.8	50.0	51.2
Method = t, DF = 20	54.2	52.8	45.8	50.0	50.7

Table: Predictive Accuracy of LDA on Validation Set.

Model Training

k-Nearest Neighbours

KNN models	Validation Periods				Average
	48 Months	36 Months	24 Months	12 Months	
k = 1	52.1	61.1	54.2	25.0	48.1
k = 2	60.4	61.1	54.2	33.3	52.3
k = 3	60.4	61.1	50.0	33.3	51.2
k = 4	52.1	52.8	50.0	25.0	45.0
k = 5	56.2	61.1	54.2	25.0	49.1
k = 6	56.2	55.6	58.3	41.7	53.0
k = 7	54.2	52.8	50.0	41.7	49.7
k = 8	45.8	52.8	50.0	41.7	47.6
k = 9	45.8	47.2	41.7	41.7	44.1
k = 10	45.8	52.8	45.8	41.7	46.5

Table: Predictive Accuracy of KNN on Validation Set.

Model Training

Support Vector Machine

SVM models	Validation Periods				Average
	48 Months	36 Months	24 Months	12 Months	
Kernel = linear, cost = 1	47.9	44.4	54.2	41.7	47.0
Kernel = linear, cost = 10	47.9	44.4	54.2	41.7	47.0
Kernel = linear, cost = 100	47.9	44.4	54.2	41.7	47.0
Kernel = radial, cost = 1	47.9	44.4	41.7	33.3	41.8
Kernel = radial, cost = 10	54.2	52.8	50.0	33.3	47.6
Kernel = radial, cost = 100	52.1	58.3	54.2	33.3	49.5
Kernel = polynomial, cost = 1	52.1	55.6	45.8	33.3	46.7
Kernel = polynomial, cost = 10	54.2	55.6	37.5	33.3	45.1
Kernel = polynomial, cost = 100	54.2	52.8	37.5	33.3	44.4
Kernel = sigmoid, cost = 1	47.9	47.2	58.3	50.0	50.9
Kernel = sigmoid, cost = 10	33.3	25.0	66.7	66.7	47.9
Kernel = sigmoid, cost = 100	33.3	30.6	29.2	58.3	37.8

Table: Predictive Accuracy of SVM on Validation Set.

Model Training

Classification Tree

CTR models	Validation Periods				Average
	48 Months	36 Months	24 Months	12 Months	
SplitCrit = information, minsize = 2	43.8	47.2	45.8	33.3	42.5
SplitCrit = information, minsize = 4	43.8	47.2	41.7	33.3	41.5
SplitCrit = information, minsize = 6	45.8	47.2	41.7	33.3	42.0
SplitCrit = information, minsize = 8	45.8	47.2	45.8	41.7	45.1
SplitCrit = information, minsize = 10	45.8	44.4	41.7	33.3	41.3
SplitCrit = gini, minsize = 2	45.8	47.2	45.8	33.3	43.1
SplitCrit = gini, minsize = 4	43.8	47.2	41.7	33.3	41.5
SplitCrit = gini, minsize = 6	45.8	47.2	41.7	33.3	42.0
SplitCrit = gini, minsize = 8	45.8	47.2	45.8	41.7	45.1
SplitCrit = gini, minsize = 10	45.8	44.4	41.7	33.3	41.3

Table: Predictive Accuracy of CTR on Validation Set.

Model Training

Random Forest

RFM models	Validation Periods				Average
	48 Months	36 Months	24 Months	12 Months	
Node size = 1, mtry = 2	52.1	52.8	45.8	33.3	46.0
Node size = 1, mtry = 3	45.8	50.0	45.8	33.3	43.8
Node size = 1, mtry = 4	45.8	50.0	45.8	33.3	43.8
Node size = 1, mtry = 5	43.8	47.2	45.8	33.3	42.5
Node size = 1, mtry = 6	45.8	47.2	41.7	33.3	42.0
Node size = 1, mtry = 7	43.8	47.2	45.8	33.3	42.5
Node size = 10, mtry = 2	54.2	58.3	45.8	33.3	47.9
Node size = 10, mtry = 3	50.0	58.3	45.8	33.3	46.9
Node size = 10, mtry = 4	52.1	58.3	45.8	33.3	47.4
Node size = 10, mtry = 5	52.1	52.8	45.8	33.3	46.0
Node size = 10, mtry = 6	50.0	52.8	45.8	33.3	45.5
Node size = 10, mtry = 7	50.0	55.6	45.8	33.3	46.2
Node size = 20, mtry = 2	58.3	52.8	37.5	33.3	45.5
Node size = 20, mtry = 3	56.2	50.0	41.7	33.3	45.3
Node size = 20, mtry = 4	58.3	52.8	41.7	33.3	46.5
Node size = 20, mtry = 5	56.2	52.8	41.7	33.3	46.0
Node size = 20, mtry = 6	56.2	52.8	41.7	33.3	46.0
Node size = 20, mtry = 7	56.2	55.6	41.7	33.3	46.7

Table: Predictive Accuracy of RFM on Validation Set.

Model Training

Extreme Gradient Boosting

XGB models	Validation Periods				Average
	48 Months	36 Months	24 Months	12 Months	
Depths = 2, eta = 0.25	50.0	47.2	45.8	50.0	48.3
Depths = 2, eta = 0.5	50.0	47.2	45.8	50.0	48.3
Depths = 2, eta = 0.75	50.0	47.2	45.8	33.3	44.1
Depths = 2, eta = 1	50.0	44.4	45.8	33.3	43.4
Depths = 3, eta = 0.25	50.0	47.2	41.7	33.3	43.1
Depths = 3, eta = 0.5	50.0	47.2	50.0	33.3	45.1
Depths = 3, eta = 0.75	47.9	44.4	45.8	33.3	42.9
Depths = 3, eta = 1	47.9	44.4	41.7	41.7	43.9
Depths = 4, eta = 0.25	43.8	44.4	45.8	41.7	43.9
Depths = 4, eta = 0.5	47.9	44.4	41.7	41.7	43.9
Depths = 4, eta = 0.75	52.1	47.2	41.7	58.3	49.8
Depths = 4, eta = 1	45.8	52.8	50.0	50.0	49.7
Depths = 5, eta = 0.25	43.8	50.0	41.7	41.7	44.3
Depths = 5, eta = 0.5	43.8	47.2	45.8	41.7	44.6
Depths = 5, eta = 0.75	56.2	47.2	41.7	50.0	48.8
Depths = 5, eta = 1	43.8	50.0	45.8	41.7	45.3

Table: Predictive Accuracy of XGB on Validation Set.

Model Training

Neural Network

RFM models	Validation Periods				Average
	48 Months	36 Months	24 Months	12 Months	
1st hidden = 2, 2nd hidden = 0	52.1	55.6	41.7	50.0	49.8
1st hidden = 3, 2nd hidden = 0	39.6	44.4	50.0	58.3	48.1
1st hidden = 4, 2nd hidden = 0	58.3	36.1	33.3	50.0	44.4
1st hidden = 5, 2nd hidden = 0	52.1	52.8	58.3	41.7	51.2
1st hidden = 2, 2nd hidden = 1	45.8	44.4	54.2	75.0	54.9
1st hidden = 3, 2nd hidden = 1	50.0	44.4	54.2	41.7	47.6
1st hidden = 4, 2nd hidden = 1	62.5	44.4	41.7	58.3	51.7
1st hidden = 5, 2nd hidden = 1	56.2	55.6	50.0	58.3	55.0
1st hidden = 2, 2nd hidden = 2	54.2	47.2	41.7	50.0	48.3
1st hidden = 3, 2nd hidden = 2	43.8	58.3	50.0	41.7	48.4
1st hidden = 4, 2nd hidden = 2	47.9	44.4	45.8	58.3	49.1
1st hidden = 5, 2nd hidden = 2	43.8	41.7	54.2	50.0	47.4

Table: Predictive Accuracy of FNN on Validation Set.

Model Training

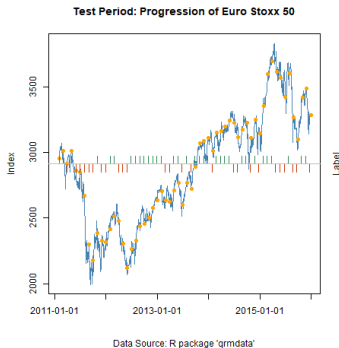
Assessment

- Classification accuracy of models roughly equivalent with coin-tossings.
- No clear improvement of correct predictions with increasing training data set.
- Results depend on models' specifications and are sensitive to those hyperparameters.
- Methods delivered in general poor results, whence evaluated on last twelve month of validation period ('sideway market environment'). In these market phases directional guidance is required the most, but ML-models did not excel (whip-saw effect).
- Lack of structural stability in data generating process might be an explanation for the rather sobering result of ML during the validation period.

Model Testing

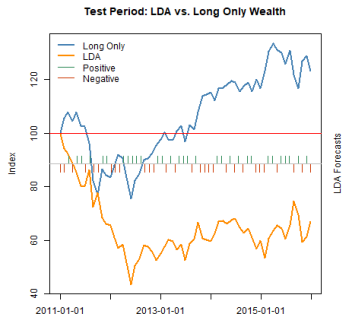
Outline

- Utilize 'optimal' model specifications determined from validation stage in test period.
- Re-estimate models based on training and validation data.
- Compute one-step ahead predictions.
- Evaluate wealth progressions by entering at the beginning of each month a position with exposure equivalent to one hundred monetary units and close position at month's end.



Model Testing

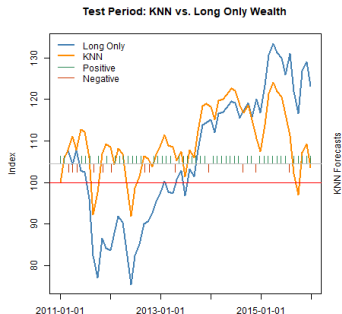
Linear Discriminant Analysis



Performance	LDA	LongOnly
Return (annualized)	-7.67	4.26
Risk (annualized)	26.04	16.74
Sharpe Ratio	-0.29	0.25
Maximum Drawdown	56.49	30.04
Average Drawdown	56.49	9.07
Hit Rate (percentage)	45.00	
False Positive (percentage)	48.39	
False Negative (percentage)	62.07	

Model Testing

k-Nearest Neighbours

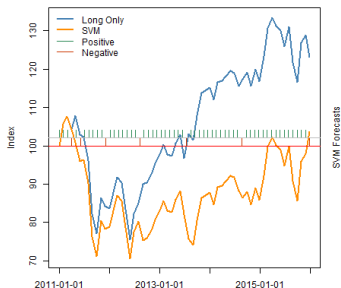


Performance	KNN	LongOnly
Return (annualized)	0.69	4.26
Risk (annualized)	15.88	16.74
Sharpe Ratio	0.04	0.25
Maximum Drawdown	21.82	30.04
Average Drawdown	11.81	9.07
Hit Rate (percentage)	48.33	
False Positive (percentage)	46.81	
False Negative (percentage)	69.23	

Model Testing

Support Vector Machine

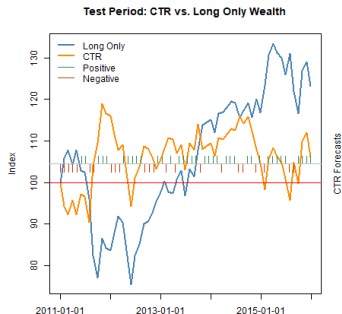
Test Period: SVM vs. Long Only Wealth



Performance	SVM	LongOnly
Return (annualized)	0.74	4.26
Risk (annualized)	19.54	16.74
Sharpe Ratio	0.04	0.25
Maximum Drawdown	34.43	30.04
Average Drawdown	34.43	9.07
Hit Rate (percentage)	55.00	
False Positive (percentage)	43.40	
False Negative (percentage)	57.14	

Model Testing

Classification Tree

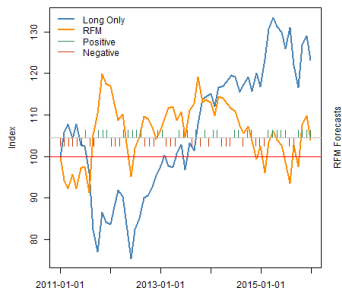


Performance	CTR	LongOnly
Return (annualized)	1.20	4.26
Risk (annualized)	16.49	16.74
Sharpe Ratio	0.07	0.25
Maximum Drawdown	20.85	30.04
Average Drawdown	15.22	9.07
Hit Rate (percentage)	45.00	
False Positive (percentage)	48.65	
False Negative (percentage)	65.22	

Model Testing

Random Forest

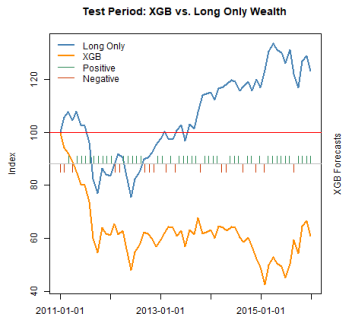
Test Period: RFM vs. Long Only Wealth



Performance	RFM	LongOnly
Return (annualized)	0.78	4.26
Risk (annualized)	16.52	16.74
Sharpe Ratio	0.05	0.25
Maximum Drawdown	22.06	30.04
Average Drawdown	15.36	9.07
Hit Rate (percentage)	45.00	
False Positive (percentage)	48.39	
False Negative (percentage)	62.07	

Model Testing

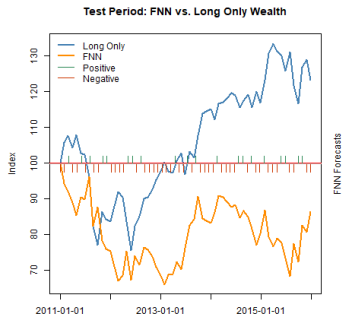
Extreme Gradient Boosting



Performance	XGB	LongOnly
Return (annualized)	-9.45	4.26
Risk (annualized)	28.53	16.74
Sharpe Ratio	-0.33	0.25
Maximum Drawdown	57.39	30.04
Average Drawdown	57.39	9.07
Hit Rate (percentage)	38.33	
False Positive (percentage)	53.49	
False Negative (percentage)	82.35	

Model Testing

Neural Network



Performance	FNN	LongOnly
Return (annualized)	-2.90	4.26
Risk (annualized)	21.02	16.74
Sharpe Ratio	-0.14	0.25
Maximum Drawdown	33.97	30.04
Average Drawdown	33.97	9.07
Hit Rate (percentage)	40.00	
False Positive (percentage)	55.00	
False Negative (percentage)	62.50	

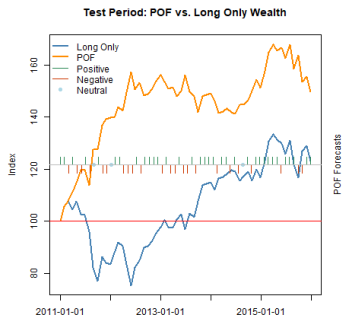
Model Testing

Neural Network: Comments

- Activation by rectified linear unit; full batch optimization (rmsprop); no dropout in layers.
- Results depend on chosen optimization engine.
- Results can be not reproducible, even if `keras::use_session_with_seed()` is used (in particular, for settings like mini-batch, stochastic gradient decent, random dropout in layers and non-fixed validation data).
- The peril of data augmentation, e.g. by adding Gaussian noise: Beforehand, models should better generalize in testing period, but how much jitter to add? If too small, then no big generalization gains are made, if too high, the labels in the training/validation set might not be any longer in sync with randomly created records.

Model Testing

'Alternative facts: these classy features are all great!' Majority voting of features³



Performance	POF	LongOnly
Return (annualized)	8.43	4.26
Risk (annualized)	11.58	16.74
Sharpe Ratio	0.73	0.25
Maximum Drawdown	10.72	30.04
Average Drawdown	6.04	9.07
Hit Rate (percentage)	64.91	
False Positive (percentage)	32.35	
False Negative (percentage)	39.13	

³Bates and Granger 1969.

Model Testing

Performance Summary

Performance	LDA	KNN	SVM	CTR	RFM	XGB	FNN	POF	LongOnly
Return (annualized)	-7.67	0.69	0.74	1.20	0.78	-9.45	-2.90	8.43	4.26
Risk (annualized)	26.04	15.88	19.54	16.49	16.52	28.53	21.02	11.58	16.74
Sharpe Ratio	-0.29	0.04	0.04	0.07	0.05	-0.33	-0.14	0.73	0.25
Maximum Drawdown	56.49	21.82	34.43	20.85	22.06	57.39	33.97	10.72	30.04
Average Drawdown	56.49	11.81	34.43	15.22	15.36	57.39	33.97	6.04	9.07
Hit Rate (percentage)	45.00	48.33	55.00	45.00	45.00	38.33	40.00	64.91	
False Positive (percentage)	48.39	46.81	43.40	48.65	48.39	53.49	55.00	32.35	
False Negative (percentage)	62.07	69.23	57.14	65.22	62.07	82.35	62.50	39.13	

Model Testing

Lifting the Veil of Secrecy

- Signs and magnitudes of Kendall correlations between predictors and label give hindsight to differing relations.
- Pooled forecasts by majority votes yield a more robust outcome compared 'trained' ML-/AI models.

Variable	All	Train	Valid	Test
EuroStoxx	1.00	1.00	1.00	1.00
Kurtosis	0.02	0.04	-0.07	0.00
RSI	-0.11	-0.10	-0.06	-0.23
RvRisk	0.00	-0.05	-0.04	0.23
SdRisk	-0.01	-0.05	-0.13	0.23
SharpeRatio	-0.01	-0.01	-0.08	0.07
Skewness	0.00	0.01	-0.09	0.03
SlopeCoef	0.08	0.09	0.07	0.03
TrendDetection	0.07	0.07	-0.04	0.18
TwoPart	-0.02	0.02	-0.15	-0.07

Summary & Conclusion

- ML-/AI methods have been applied to a binary classification problem.
- All tested methods showed inferior results compared to either a long-only and/or pooled majority forecasts of the predictors.
- Potential reason for this empirical finding is a lack of structural stability across training, validation and testing periods.
- In this sense: 'a euro is not a euro'.
- So, 'Will this second wave last ...?': Probably not in the field of empirical social science, but in fairly stable and structured domains e.g. in which 'a cat is still a cat'.

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